# Supplemental Material: Cluster-Aware Grid Layout 

Category: Research

Paper Type: algorithm/technique

## 1 USER STUDY DETAILS

A user study is presented in Section 3.1 of the paper. We report here the content of the tutorial shown to participants, the trials used in practice session and formal study and the questionnaire.

### 1.1 Tutorial and practice trials

We present a tutorial video to participants that introduced the definition of convex polygons and the user interface of the study system. Here is the content of the tutorial.

What is a convex polygon? Convex polygons refer to polygons whose internal angles are less than or equal 180 degrees.(Fig. 1) Triangles are convex polygons because all internal angles are less than 180 degrees. Besides, regular polygons are always convex. However, quadrilateral may be non-convex according to the degree of internal angles.(Fig. 2)

Convex Polygons
Convex polygons refer to polygons whose internal angles are less than or equal 180 degrees.


Fig. 1: Convex polygons.

## Examples

Quadrilateral may be non-convex according to the degree of internal angles.


Fig. 2: Example of polygons.

What is convexity? Convexity describes how close a shape is to a convex shape. For non-convex polygons, there are also polygons with better convexity or worse convexity.(Fig. 3) Some examples are given to show polygons with different convexity. It can be seen that as the number and magnitude of depressions become smaller, the convexity of the polygon from left to right becomes better. (Fig. 4)

## Convexity

For non-convex polygons, there are also polygons with better convexity or worse convexity.
Convexity is one of the basic descriptors of shape.


Fig. 3: Convexity.

## Examples



Fig. 4: Example of polygons with different convexity.

How to use the study system? The system of user study is introduced in the tutorial. (Fig. 5) Four different grid visualizations are displayed in the system. Users need to click and sort grid visualizations according to their understanding of convexity. The sorting results will be displayed below. Users can drag and drop to modify the sorting results, or click ">" to modify it to " $=$ " which indicate that the convexity of the visualizations on the left and right sides are similar. After completing a question, the user can click the next button to proceed to the next question. If the user wants to modify the previous result, he can click the previous button to return to the previous question. We also provide a clear button to clear current answers.


Fig. 5: Example interface of the user study.

Practice trials In the practice session, six practice trials were presented to participants to familiarize them with the concept of convexity and the use of the system. After completing each exercise question, the system will check the answer and present the correct result of the question. At the same time, the positions that mainly affects the convexity of the visualization will be marked in red ink in the figure to help users understand the convexity. Fig. 6 show these practice trials.


Fig. 6: Practice trials.

### 1.2 Formal study trials

In the formal session, a total of 36 trials ( 3 grid sizes $\times 3$ cluster numbers $\times 4$ datasets) were evaluated. Fig. 7 - Fig. 10 show these trials.


Fig. 7: Trials from dataset Animals [4].


Fig. 8: Trials from dataset Cifar10 [9].


Fig. 9: Trials from dataset Mnist [10].


Fig. 10: Trials from dataset USPS [7]

### 1.3 Questionnaire

Following the completion of all trials, participants were asked to fill out a questionnaire that included personal information and a question asking them to explain how they compare the convexity of different grid visualizations.

## Part One: Basic Information

1. Please select the range of your age.

$$
16-20
$$21-2526-3031-3536-4041-4546-5051-5556-60More than 60

2. Please select your gender.MaleFemale
3. Please select your education background.High school and belowBachelorMaster's degreeDoctoral degree
4. Whether you have color blindness, color weakness or other diseases that affect visual judgment?NoYes, illegible colors: $\qquad$
5. Please specify your contact information. (telephone/email)
$\qquad$

## Part Two: Professional background

6. Are you familiar with the concepts of convexity and convex polygons?
Unfamiliar / Slightly familiar / Moderately familiar / Familiar / Very familiar
Unfamiliar $\qquad$ $\square$ $\square$ $-\square$ $-\square$ Very familiar
7. Are you familiar with grid layouts?

Unfamiliar $\qquad$ - $\square$
$\qquad$ - $\square$ $\square-\square$ $\square-$Very familiar

## Part Three: Open question

8. How did you judge the convexity of graphics in the formal trials?
For example, in the example below, among the factors such as the slope of the edge, the degree of curvature, the number of serrations, the number and size of the depressions, etc., which help you judge whether the grid layout has better/worse convexity?


Fig. 11: Example
$\qquad$
$\qquad$

## 2 EXPERIMENTS DETAILS

### 2.1 Datasets

Ten datasets we used are from Xia et al. 's work [12]. They are Animals [4], CIFAR10 [9], Indian Food [11], Isolet [5], MNIST [10], Stanford Dogs [3], Texture [1], USPS [7], Weather [6] and Wifi [2]. We also used an additional dataset, OoD-Animals, which is from a real-world application [3].
It is about different images of different animals: cat, dog, rabbit, wolf, and tiger. The information of datasets are shown in Table 1.

Table 1: Datasets information.

| Dataset | Size | Clusters | Type |
| :--- | ---: | ---: | ---: |
| Animals [4] | 26179 | 10 | Image |
| CIFAR10 [9] | 60000 | 10 | Image |
| Indian Food [11] | 3625 | 11 | Image |
| Isolet [5] | 2352 | 8 | Text |
| MNIST [10] | 70000 | 10 | Image |
| Stanford Dogs [8] | 1291 | 7 | Image |
| Texture [1] | 5500 | 11 | Text |
| USPS [7] | 9298 | 10 | Image |
| Weather [6] | 1156 | 4 | Image |
| Wifi [2] | 2000 | 4 | Tabular |
| OoD-Animals [3] | 26683 | 5 | Image |

### 2.2 Pearson Correlations Between Convexity Measures

The correlation between convexity measures is calculated based on a set of diverse cluster shapes. Therefore, the key is to generate a diverse set of cluster shapes that are similar to those that appear in a grid layout. To achieve this, we generated multiple grid layouts using the baseline method and then extracted the shape of each cluster. Specifically, we used the ten datasets from Xia et al. 's work [12], and generated 60 grid layouts using the baseline with each grid size $(20 \times 20$, $30 \times 30,40 \times 40$ ). Thus, we obtained $10 \times 60 \times 3=1800$ grid layouts and then extracted corresponding cluster shapes. If a cluster contained multiple disconnected components, we would only choose the largest connected one because those disconnected components usually have poor convexity at all measures, which cannot help evaluate the correlation between different measures. In total, 9,689 different shapes are selected to evaluate the correlations between convexity measures.

### 2.3 Full Experiment Results in Evaluation

Layout generation. For each dataset, we began by sampling 20x20, $30 \times 30$, and $40 \times 40$ samples for each dataset. We then generated t-SNE projections from these samples and used them as input for the baseline layout method. However, because different rotations of the same t-SNE projection can produce different grid layouts, we rotated each projection with degrees $\pi / 16 * k, k=0,1, \ldots, 7$. To reduce the randomness in sampling, we repeated this entire process five times. As a result, we generated a total of 120 layouts for each dataset ( 3 sizes x 8 rotations x 5 repetitions).
Results. In the ablation study, Tables 2 to 7 show the comparison of proximity, compactness, area ratio, triple ratio, perimeter ratio, and cut ratio of all the methods on 11 datasets. The results are averaged over different grid sizes. To demonstrate the effectiveness of our method, Tables 8 to 10 show the comparison of proximity, compactness, area ratio, triple ratio, perimeter ratio, and cut ratio between baseline and Ours-T/Ours-P on 11 datasets with 3 different grid sizes.

### 2.4 Examples

Here are examples of layouts generated by baseline method and our method, from different datasets.

## Animals



Fig. 12

## Cifar 10



Fig. 13
Indian Food

Baseline


Ours-T


Ours-G


Fig. 14


Fig. 15


Fig. 16


Ours-T


Fig. 17


Baseline


Ours-T


Ours-G


Ours-P


Fig. 18

## USPS

Baseline


Ours-T


Ours-G


Fig. 19

Fig. 20

Wifi


Ours-T


Ours-G


Ours-P


Fig. 21

## OoD-Animals

Baseline
Ours-G


|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |



Fig. 22

Table 2: Comparison of proximity of all the methods. G: global; L: local; T: triple ratio; P: perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Animals | $\mathbf{1 . 0 0 0}$ | 0.998 | 0.999 | 0.995 | 0.999 | 0.998 | 0.998 |  |
| CIFAR10 | $\mathbf{1 . 0 0 0}$ | 0.999 | 0.999 | 0.996 | 0.999 | 0.999 | 0.999 | 0.996 |
| Indian Food | $\mathbf{1 . 0 0 0}$ | 0.996 | 0.997 | 0.989 | 0.997 | 0.996 | 0.995 |  |
| Isolet | $\mathbf{1 . 0 0 0}$ | 0.995 | 0.997 | 0.992 | 0.995 | 0.995 | 0.995 | 0.998 |
| MNIST | $\mathbf{1 . 0 0 0}$ | 0.998 | 0.999 | 0.993 | 0.999 | 0.998 | 0.994 |  |
| Stanford Dogs | $\mathbf{1 . 0 0 0}$ | 0.996 | 0.996 | 0.988 | 0.996 | 0.996 | 0.995 | 0.996 |
| Texture | $\mathbf{1 . 0 0 0}$ | 0.996 | 0.998 | 0.990 | 0.996 | 0.996 | 0.992 |  |
| USPS | $\mathbf{1 . 0 0 0}$ | 0.998 | 0.999 | 0.994 | 0.999 | 0.998 | 0.998 |  |
| Weather | $\mathbf{1 . 0 0 0}$ | 0.992 | 0.998 | 0.991 | 0.997 | 0.992 | 0.991 |  |
| Wifi | $\mathbf{1 . 0 0 0}$ | 0.991 | 0.998 | 0.994 | 0.992 | 0.991 | 0.991 |  |
| OoD-Animals | $\mathbf{1 . 0 0 0}$ | 0.998 | 0.998 | 0.989 | 0.998 | 0.997 | 0.997 |  |
| Average | $\mathbf{1 . 0 0 0}$ | 0.996 | 0.998 | 0.992 | 0.997 | 0.996 | 0.996 |  |

Table 3: Comparison of compactness of all the methods. G: global; L: local; T: triple ratio; P: perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Animals | 0.974 | $\mathbf{0 . 9 7 7}$ | 0.975 | 0.973 | 0.976 | 0.976 |  |  |
| CIFAR10 | 0.980 | $\mathbf{0 . 9 8 1}$ | 0.980 | 0.978 | $\mathbf{0 . 9 8 1}$ | $\mathbf{0 . 9 7 7}$ | $\mathbf{0 . 9 7 7}$ | $\mathbf{0 . 9 8 1}$ |
| Indian Food | 0.970 | $\mathbf{0 . 9 7 8}$ | 0.976 | 0.970 | 0.977 | $\mathbf{0 . 9 7 8}$ | $\mathbf{0 . 9 7 1}$ |  |
| Isolet | 0.965 | $\mathbf{0 . 9 7 3}$ | 0.969 | 0.963 | $\mathbf{0 . 9 7 3}$ | $\mathbf{0 . 9 7 3}$ | $\mathbf{0 . 9 7 3}$ |  |
| MNIST | 0.977 | $\mathbf{0 . 9 8 0}$ | 0.979 | 0.975 | $\mathbf{0 . 9 8 0}$ | $\mathbf{0 . 9 8 0}$ | $\mathbf{0 . 9 8 0}$ |  |
| Stanford Dogs | 0.960 | $\mathbf{0 . 9 6 9}$ | 0.967 | 0.960 | $\mathbf{0 . 9 6 9}$ | $\mathbf{0 . 9 6 9}$ | $\mathbf{0 . 9 6 9}$ |  |
| Texture | 0.973 | $\mathbf{0 . 9 7 9}$ | 0.976 | 0.970 | $\mathbf{0 . 9 7 9}$ | $\mathbf{0 . 9 7 9}$ | $\mathbf{0 . 9 7 9}$ |  |
| USPS | 0.976 | $\mathbf{0 . 9 7 9}$ | 0.977 | 0.974 | 0.978 | $\mathbf{0 . 9 7 9}$ |  |  |
| Weather | 0.936 | $\mathbf{0 . 9 4 4}$ | 0.939 | 0.937 | 0.940 | 0.979 |  |  |
| Wifi | 0.939 | $\mathbf{0 . 9 5 0}$ | 0.942 | 0.937 | 0.949 | 0.967 |  |  |
| OoD-Animals | 0.953 | $\mathbf{0 . 9 6 0}$ | 0.959 | 0.952 | $\mathbf{0 . 9 6 0}$ | 0.949 | $\mathbf{0 . 9 7 9}$ | $\mathbf{0 . 9 4 9}$ |
| Average | 0.964 | $\mathbf{0 . 9 7 0}$ | 0.967 | 0.963 | 0.969 | $\mathbf{0 . 9 5 4}$ | 0.978 |  |

Table 4: Comparison of area ratio of all the methods. G : global; $\mathrm{L}:$ local; T : triple ratio; P : perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Animals | 0.775 | 0.893 | 0.897 | 0.872 | 0.884 | 0.896 | 0.910 | 0.900 |
| CIFAR10 | 0.786 | 0.893 | 0.899 | 0.869 | 0.885 | 0.893 | 0.910 | 0.901 |
| Indian Food | 0.555 | 0.846 | 0.889 | 0.818 | 0.832 | 0.840 | 0.901 | 0.885 |
| Isolet | 0.593 | 0.867 | 0.886 | 0.827 | 0.855 | 0.870 | 0.905 | 0.891 |
| MNIST | 0.718 | 0.886 | 0.899 | 0.868 | 0.862 | 0.884 | 0.908 | 0.901 |
| Stanford Dogs | 0.577 | 0.860 | 0.907 | 0.846 | 0.851 | 0.858 | 0.919 | 0.890 |
| Texture | 0.617 | 0.856 | 0.877 | 0.819 | 0.851 | 0.858 | 0.889 | 0.870 |
| USPS | 0.739 | 0.892 | 0.896 | 0.875 | 0.877 | 0.891 | 0.910 | 0.904 |
| Weather | 0.738 | 0.903 | 0.906 | 0.872 | 0.874 | 0.918 | 0.926 | 0.877 |
| Wifi | 0.724 | 0.921 | 0.916 | 0.845 | 0.915 | 0.921 | 0.936 | 0.916 |
| OoD-Animals | 0.534 | 0.889 | 0.924 | 0.862 | 0.877 | 0.886 | 0.932 | 0.914 |
| Average | 0.669 | 0.882 | 0.900 | 0.852 | 0.869 | 0.883 | 0.913 | 0.895 |

Table 5: Comparison of triple ratio of all the methods. G: global; L: local; T: triple ratio; P: perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Animals | 0.977 | 0.995 | 0.996 | 0.973 | 0.994 | 0.995 | $\mathbf{0 . 9 9 7}$ | 0.983 |
| CIFAR10 | 0.975 | 0.994 | 0.996 | 0.961 | 0.993 | 0.994 | 0.979 |  |
| Indian Food | 0.889 | 0.986 | 0.996 | 0.947 | 0.985 | 0.984 | $\mathbf{0 . 9 9 7}$ | $\mathbf{0 . 9 9 7}$ |
| Isolet | 0.893 | 0.986 | 0.993 | 0.936 | 0.983 | 0.987 | $\mathbf{0 . 9 9 6}$ |  |
| MNIST | 0.963 | 0.993 | 0.996 | 0.964 | 0.989 | 0.991 | $\mathbf{0 . 9 9 7}$ | 0.974 |
| Stanford Dogs | 0.909 | 0.984 | 0.997 | 0.949 | 0.983 | 0.983 | 0.982 |  |
| Texture | 0.893 | 0.985 | 0.991 | 0.929 | 0.983 | 0.985 | $\mathbf{0 . 9 9 8}$ | 0.976 |
| USPS | 0.968 | 0.995 | 0.996 | 0.971 | 0.992 | 0.994 | $\mathbf{0 . 9 9 4}$ |  |
| Weather | 0.952 | 0.993 | 0.995 | 0.963 | 0.989 | 0.996 | $\mathbf{0 . 9 9 7}$ |  |
| Wifi | 0.953 | 0.997 | 0.996 | 0.944 | 0.996 | 0.997 | $\mathbf{0 . 9 9 7}$ | 0.984 |
| OoD-Animals | 0.925 | 0.993 | $\mathbf{0 . 9 9 8}$ | 0.961 | 0.993 | 0.993 | $\mathbf{0 . 9 9 8}$ |  |
| Average | 0.936 | 0.991 | 0.995 | 0.954 | 0.989 | 0.965 |  |  |

Table 6: Comparison of perimeter ratio of all the methods. G: global; L: local; T: triple ratio; P: perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Animals | 0.830 | 0.859 | 0.853 | 0.926 | 0.851 | 0.861 | 0.872 | $\mathbf{0 . 9 3 5}$ |
| CIFAR10 | 0.834 | 0.855 | 0.850 | 0.925 | 0.850 | 0.853 | $\mathbf{0 . 9 3 4}$ |  |
| Indian Food | 0.807 | 0.804 | 0.854 | 0.916 | 0.809 | 0.800 | 0.861 | $\mathbf{0 . 9 2 9}$ |
| Isolet | 0.784 | 0.818 | 0.858 | 0.921 | 0.818 | 0.824 | 0.864 | 0.864 |
| MNIST | 0.852 | 0.845 | 0.858 | 0.926 | 0.844 | 0.844 | 0.868 |  |
| Stanford Dogs | 0.868 | 0.773 | 0.854 | 0.926 | 0.777 | 0.772 | $\mathbf{0 . 9 3 6}$ |  |
| Texture | 0.794 | 0.828 | 0.857 | 0.922 | 0.828 | 0.833 | 0.850 |  |
| USPS | 0.861 | 0.851 | 0.854 | 0.930 | 0.846 | 0.850 | 0.865 |  |
| Weather | 0.790 | 0.858 | 0.863 | $\mathbf{0 . 9 4 0}$ | 0.849 | 0.880 | 0.864 |  |
| Wifi | 0.784 | 0.867 | 0.861 | 0.929 | 0.867 | 0.867 | 0.875 |  |
| OoD-Animals | 0.724 | 0.812 | 0.862 | 0.929 | 0.825 | 0.807 | 0.873 |  |
| Average | 0.812 | 0.834 | 0.857 | 0.926 | 0.833 | 0.835 | $\mathbf{0 . 9 2 7}$ |  |

Table 7: Comparison of cut ratio of all the methods. G: global; L: local; T: triple ratio; P: perimeter ratio.

| Dataset | Baseline | Ours-G | Ours-L(A) | Ours-L(B) | Ours-L(A)-G | Ours-L(B)-G | Ours-G-L(A) | Ours-G-L(B) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Animals | 0.838 | 0.887 | 0.872 | 0.920 | 0.879 | 0.888 | 0.895 | 0.936 |
| CIFAR10 | 0.843 | 0.890 | 0.876 | 0.920 | 0.883 | 0.889 | 0.899 | 0.937 |
| Indian Food | 0.763 | 0.849 | 0.867 | 0.893 | 0.846 | 0.844 | 0.885 | 0.925 |
| Isolet | 0.776 | 0.858 | 0.868 | 0.901 | 0.855 | 0.861 | 0.885 | 0.932 |
| MNIST | 0.848 | 0.887 | 0.889 | 0.918 | 0.882 | 0.886 | 0.900 | 0.936 |
| Stanford Dogs | 0.786 | 0.836 | 0.872 | 0.912 | 0.835 | 0.835 | 0.893 | 0.931 |
| Texture | 0.781 | 0.856 | 0.860 | 0.898 | 0.855 | 0.860 | 0.870 | 0.921 |
| USPS | 0.839 | 0.888 | 0.878 | 0.922 | 0.879 | 0.887 | 0.898 | 0.937 |
| Weather | 0.803 | 0.862 | 0.856 | 0.927 | 0.852 | 0.889 | 0.868 | 0.927 |
| Wifi | 0.800 | 0.890 | 0.866 | 0.910 | 0.889 | 0.890 | 0.896 | 0.947 |
| OoD-Animals | 0.744 | 0.868 | 0.892 | 0.920 | 0.870 | 0.865 | 0.904 | 0.946 |
| Average | 0.802 | 0.870 | 0.872 | 0.913 | 0.866 | 0.872 | 0.890 | 0.934 |

Table 8: Comparison of four convexity measures on 11 datasets with grid size of $20 \times 20$.

| Dataset | mit |  |  | mpactness |  |  | Area ratio |  |  | Triple |  |  |  |  |  | Cut ratio |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Ours-T | Ours-P | Basel. | Ours | Ou |  | Ours | P |  | Ours | O | Base | Ours | Ours-P | Base |  | urs-P |
|  | 1.0 | 0.998 | 99 | 0. | 0.9 | 0.975 | 0.8 | 0.8 | 0.89 | 0.981 | 0.9 | 0.980 | 0.840 | 0.878 | 0.93 | 0.860 | 0.896 | 0.932 |
| FAR10 | 1.000 | 0.999 | 0.996 | 0.980 | 0.981 | 0.979 | 0.831 | 0.892 | 0.891 | 0.979 | 0.995 | 0.973 | 0.832 | 0.873 | 0.934 | 0.859 | 0.897 | 0.932 |
| Indian Food | 1.000 | 0.997 | 0.995 | 0.975 | 0.979 | 0.977 | 0.720 | 0.893 | 0.898 | 0.944 | 0.996 | 0.983 | 0.843 | 0.874 | 0.936 | 0.831 | 0.899 | 0.934 |
| Isolet | 1.000 | 0.995 | 0.994 | 0.968 | 0.974 | 0.972 | 0.696 | 0.893 | 0.888 | 0.920 | 0.994 | 0.973 | 0.838 | 0.874 | 0.935 | 0.826 | 0.894 | 0.931 |
| NIST | 1.000 | 0.998 | 0.995 | 0.977 | 0.980 | 0.978 | 0.746 | 0.891 | 0.891 | 0.95 | 0.995 | 0.975 | 0.863 | 0.87 | 0.934 | 0.86 | 0.901 | 0.932 |
| Stanford | 1.000 | 0.995 | 0.991 | 0.961 | 0.969 | 0.967 | 0.64 | 0.907 | 0.89 | 0.91 | 0.99 | 0.97 | 0.89 | 0.87 | 0.93 | 0.81 | 0.901 | 0.934 |
| Texture | 1.000 | 0.995 | 0.994 | 0.974 | 0.980 | 0.977 | 0.733 | 0.869 | 0.865 | 0.925 | 0.990 | 0.956 | 0.848 | 0.857 | 0.929 | 0.837 | 0.874 | 0.920 |
| USPS | 1.000 | 0.997 | 0.995 | 0.976 | 0.979 | 0.978 | 0.777 | 0.895 | 0.895 | 0.969 | 0.995 | 0.981 | 0.867 | 0.876 | 0.932 | 0.860 | 0.902 | 0.933 |
| Weathe | 1.000 | 0.995 | 0.988 | 0.939 | 0.942 | 0.940 | 0.824 | 0.909 | 0.907 | 0.973 | 0.995 | 0.977 | 0.844 | 0.877 | 0.949 | 0.847 | 0.878 | 0.944 |
| Wifi | 1.000 | 0.991 | 0.989 | 0.942 | 0.950 | 0.948 | 0.824 | 0.924 | 0.912 | 0.974 | 0.997 | 0.979 | 0.834 | 0.884 | 0.947 | 0.844 | 0.901 | 0.945 |
| OoD-Animals | 1.000 | 0.997 | 0.993 | 0.953 | 0.960 | 0.95 | 0.624 | 0.918 | 0.915 | 0.922 | 0.997 | 0.985 | 0.767 | 0.879 | 0.944 | 0.781 | 0.907 | 0.94 |
| verage | 1.000 | . 99 | 0.99 | 0.9 | . 9 | 0.968 | 0.75 | 0.89 | 0.89 | 0.95 | 0.995 | 0.976 | 0.84 | 0.875 | 0.938 | 0.83 | 0.895 | 0.93 |

Table 9: Comparison of four convexity measures on 11 datasets with grid size of $30 \times 30$.

| Dataset | Proximity |  |  | Compactness |  |  | Area ratio |  |  | Triple ratio |  |  | Perimeter ratio |  |  | Cut ratio |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bas | Ours-T | Ours-P | Basel. | Ours-T | Ours-P | Basel. | Ours-T | Ours-P | Basel. | Ours-T | Ours-P | Basel. | Ours-T | Ours-P | Basel. | Ours-T | Ours-P |
| Animals | 1.000 | 0.998 | 0.996 | 0.974 | 0.977 | 0.977 | 0.767 | 0.912 | 0.900 | 0.976 | 0.997 | 0.983 | 0.834 | 0.871 | 0.934 | 0.838 | 0.896 | 0.936 |
| CIFAR10 | 1.000 | 0.999 | 0.997 | 0.980 | 0.981 | 0.981 | 0.799 | 0.914 | 0.904 | 0.978 | 0.997 | 0.981 | 0.839 | 0.870 | 0.934 | 0.849 | 0.901 | 0.939 |
| Indian Food | 1.000 | 0.996 | 0.995 | 0.971 | 0.978 | 0.977 | 0.542 | 0.905 | 0.892 | 0.893 | 0.997 | 0.985 | 0.808 | 0.861 | 0.929 | 0.758 | 0.887 | 0.927 |
| Isolet | 1.000 | 0.995 | 0.993 | 0.965 | 0.973 | 0.971 | 0.592 | 0.906 | 0.892 | 0.888 | 0.996 | 0.975 | 0.775 | 0.861 | 0.936 | 0.772 | 0.883 | 0.932 |
| MNIST | 1.000 | 0.998 | 0.997 | 0.978 | 0.981 | 0.980 | 0.738 | 0.911 | 0.907 | 0.973 | 0.997 | 0.985 | 0.856 | 0.865 | 0.934 | 0.857 | 0.902 | 0.939 |
| Stanford Dogs | 1.000 | 0.995 | 0.993 | 0.960 | 0.969 | 0.967 | 0.557 | 0.922 | 0.889 | 0.911 | 0.998 | 0.975 | 0.889 | 0.868 | 0.931 | 0.787 | 0.895 | 0.930 |
| Texture | 1.000 | 0.996 | 0.995 | 0.973 | 0.980 | 0.978 | 0.636 | 0.893 | 0.877 | 0.908 | 0.995 | 0.969 | 0.805 | 0.848 | 0.928 | 0.784 | 0.871 | 0.923 |
| USPS | 1.000 | 0.998 | 0.997 | 0.976 | 0.979 | 0.978 | 0.758 | 0.911 | 0.905 | 0.975 | 0.998 | 0.986 | 0.864 | 0.863 | 0.933 | 0.845 | 0.898 | 0.937 |
| Weather | 1.000 | 0.990 | 0.987 | 0.937 | 0.945 | 0.942 | 0.726 | 0.930 | 0.872 | 0.951 | 0.997 | 0.961 | 0.787 | 0.861 | 0.936 | 0.797 | 0.865 | 0.924 |
| Wifi | 1.000 | 0.991 | 0.988 | 0.939 | 0.950 | 0.948 | 0.702 | 0.939 | 0.921 | 0.952 | 0.998 | 0.986 | 0.789 | 0.875 | 0.949 | 0.795 | 0.898 | 0.950 |
| OoD-Animals | 1.000 | 0.997 | 0.994 | 0.953 | 0.960 | 0.959 | 0.488 | 0.933 | 0.914 | 0.919 | 0.998 | 0.984 | 0.731 | 0.871 | 0.944 | 0.734 | 0.903 | 0.945 |
| Average | 1.000 | 0.996 | 0.994 | 0.964 | 0.970 | 0.969 | 0.664 | 0.916 | 0.897 | 0.938 | 0.997 | 0.979 | 0.816 | 0.865 | 0.935 | 0.801 | 0.891 | 0.935 |

Table 10: Comparison of four convexity measures on 11 datasets with grid size of $40 \times 40$.

| Dataset | Proximity |  |  | Compactness |  |  | Area ratio |  |  | Triple ratio |  |  | Perimeter ratio |  |  | Cut ratio |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Basel. |  |  | Basel. |  | Ou | Basel. | Ours- | Ours-P | Basel. | Ours-T | Ou | Basel. | Ours-T | Our | Basel. | Ours-T | Ours-P |
| Animals | 1.000 | 0.998 | 0.996 | 0.974 | 0.977 | 0.977 | 0.726 | 0.925 | 0.906 | 0.975 | 0.998 | 0.986 | 0.816 | 0.866 | 0.935 | 0.816 | 0.894 | 0.939 |
| CIFAR10 | 1.000 | 0.999 | 0.998 | 0.979 | 0.981 | 0.981 | 0.727 | 0.924 | 0.907 | 0.969 | 0.998 | 0.984 | 0.830 | 0.861 | 0.935 | 0.820 | 0.898 | 0.940 |
| Indian Food | 1.000 | 0.993 | 0.992 | 0.965 | 0.977 | 0.975 | 0.403 | 0.906 | 0.864 | 0.830 | 0.998 | 0.976 | 0.769 | 0.848 | 0.922 | 0.701 | 0.868 | 0.913 |
| Isolet | 1.000 | 0.994 | 0.993 | 0.963 | 0.973 | 0.971 | 0.491 | 0.917 | 0.892 | 0.870 | 0.997 | 0.974 | 0.740 | 0.855 | 0.938 | 0.731 | 0.877 | 0.932 |
| MNIST | 1.000 | 0.998 | 0.997 | 0.977 | 0.981 | 0.980 | 0.670 | 0.922 | 0.905 | 0.960 | 0.998 | 0.985 | 0.838 | 0.855 | 0.931 | 0.828 | 0.896 | 0.938 |
| Stanford Dogs | 1.000 | 0.995 | 0.993 | 0.960 | 0.969 | 0.968 | 0.529 | 0.928 | 0.886 | 0.904 | 0.998 | 0.977 | 0.816 | 0.858 | 0.931 | 0.753 | 0.884 | 0.929 |
| Texture | 1.000 | 0.995 | 0.994 | 0.970 | 0.979 | 0.977 | 0.481 | 0.905 | 0.869 | 0.845 | 0.996 | 0.966 | 0.729 | 0.844 | 0.925 | 0.720 | 0.867 | 0.919 |
| USPS | 1.000 | 0.998 | 0.997 | 0.975 | 0.979 | 0.978 | 0.682 | 0.923 | 0.912 | 0.960 | 0.998 | 0.988 | 0.851 | 0.857 | 0.934 | 0.813 | 0.894 | 0.940 |
| Weather | 1.000 | 0.988 | 0.986 | 0.934 | 0.945 | 0.942 | 0.662 | 0.939 | 0.852 | 0.931 | 0.998 | 0.957 | 0.739 | 0.856 | 0.927 | 0.766 | 0.860 | 0.912 |
| Wifi | 1.000 | 0.991 | 0.989 | 0.937 | 0.949 | 0.947 | 0.645 | 0.946 | 0.916 | 0.933 | 0.999 | 0.982 | 0.728 | 0.867 | 0.948 | 0.761 | 0.891 | 0.946 |
| OoD-Animals | 1.000 | 0.998 | 0.995 | 0.954 | 0.960 | 0.959 | 0.489 | 0.945 | 0.914 | 0.934 | 0.999 | 0.983 | 0.672 | 0.869 | 0.943 | 0.718 | 0.902 | 0.946 |
| Average | 1.000 | 0.995 | 0.993 | 0.962 | 0.970 | 0.969 | 0.591 | 0.926 | 0.893 | 0.919 | 0.998 | 0.978 | 0.775 | 0.858 | 0.933 | 0.766 | 0.885 | 0.932 |

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