Supplemental Material: Dynamic Color Assignment for Hierarchical Data

1 DATASETS

[Tab. S1](#page-0-0) presents the detailed information of 12 datasets used in our qualitative evaluation, including the number of classes and the number of samples. The first six datasets are flat datasets with a moderate range of classes, which are used to evaluate flat color assignment methods. The remaining six datasets have a larger number of classes, which are used to evaluate hierarchical color assignment methods.

Table S1: The information of the datasets.

Dataset	# Classes	# Samples		
MNIST $[11]$	10	70,000		
Animals [4]	10	26, 179		
Indian Food [13]	13	4,770		
Clothing [21]	14	37,497		
Texture $[1]$	15	5,500		
Isolet $[7]$	26	7,797		
Food101 [2]	101	101,000		
Flowers 102 [14]	102	8,189		
Stanford Cars [10]	196	16, 185		
Caltech 256 [9]	257	30,607		
Nabirds [18]	555	48,000		
ImageNet1k [5]	1,000	1,281,167		

2 RUNNING TIME

We evaluated the running time of our method on a Linux server with an Intel i9-13900K CPU (3.0 GHz). The running time consists of two parts: 1) time for computing nearest neighbors for the spatial distribution term and 2) time for optimizing color assignment results using simulated annealing. The first part depends on the dataset size. As shown in Table [S2,](#page-0-1) it takes less than 0.2 seconds to compute the nearest neighbors for 100,000 samples in a scatterplot. The second part is independent of the dataset size but depends on the number of classes. As shown in Table [S3,](#page-0-2) our algorithm can assign colors to 20 classes within 0.4 seconds and to 30 classes within 1 second. Previous research has shown that a color palette with 26 colors already exhibits poor discriminability [\[6\]](#page-5-12). Therefore, our method well supports realtime interaction for users navigating through hierarchical visualizations. Table [S3](#page-0-2) further details the processing times for different stages. Most of the time is spent on the first stage to enhance discriminability, with subsequent optimization stages achieving rapid convergence.

3 ADDITIONAL COLOR ASSIGNMENT RESULTS

In this section, we offer four additional examples that compare hierarchical color assignment results, each corresponding to one of the four visualization types.

Table S2: Average running time (in seconds) of computing nearest neighbors in scatterplots with different numbers of samples.

#Sample	1,000	10,000	100,000
Time	0.002	0.014	0.171

Table S3: Average running time (in seconds) of optimizing color assignment results in each stage.

Palette. The generation of the palette does not incorporate the spatial distribution information of the data. As users explore, the colors corresponding to child classes are generated solely based on the colors of their parent classes. [Fig. S1](#page-1-0) presents an example where users explore a lower hierarchical level. The colors on the left side of the dividing line are the colors of the parent classes, while the colors on the right side are the colors of their child classes. It can be observed that Color Crafting [\[16\]](#page-5-13) and Tree Colors [\[17\]](#page-5-14) produce many similar colors, resulting in poor discriminability. Meanwhile, Palettailor [\[12\]](#page-5-15) and Cuttlefish [\[19\]](#page-5-16) perform poorly in the alignment with hierarchy, making it difficult for users to associate parent and child classes. Our approach improves discriminability and harmony while ensuring consistency, yielding relatively satisfactory results.

Scatterplot. We adopt the approach proposed by Xiang *et al*. [\[20\]](#page-5-17) to generate hierarchical scatterplots. It employs incremental t-SNE to dynamically generate scatterplots for each layer. We then apply the color assignment results generated by different methods. [Fig. S2](#page-1-1) presents an example where users explore a higher hierarchical level. It can be observed that almost all baseline methods do not perform sufficiently well in discriminability, with colors that are difficult to distinguish. While Palettailor performs relatively well, there are still some colors that cannot be differentiated. In contrast, our method ensures discriminability and improves color harmony.

Parallel coordinates. We adopt the approach proposed by Fua *et al*. [\[8\]](#page-5-18) to generate hierarchical parallel coordinates. [Fig. S3](#page-1-2) presents an example where users explore a higher hierarchical level. The high quantity and complexity of the lines demand high discriminability for quality color assignment. Our method is relatively well-suited to adapt to such situations.

Grid visualization. We utilized the approach proposed by Chen [\[3\]](#page-5-19) to generate hierarchical grid visualizations. Compared to scatterplots and parallel coordinates, grid visualizations using surfaces can more easily display colors. [Fig. S4](#page-1-3) presents an example where users explore a higher hierarchical level. It can be seen that our method exhibits relatively high discriminability and harmony. In comparison, the result of Cuttlefish [\[19\]](#page-5-16) is harmonic but contains very similar colors.

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Fig. S3: An example of exploring a higher hierarchical level in the form of parallel coordinates.

Fig. S4: An example of exploring a higher hierarchical level in the form of grid visualization.

 (e) Ours-S

Fig. S1: An example of exploring a lowerw hierarchical level in the form of the color palette. Since spatial distribution is not considered, Ours-S and Ours-D generate the same result.

Fig. S2: An example of exploring a higher hierarchical level in the form of scatterplot.

Table S4: Comparison of our method with the representative color assignment methods for flat color assignment, with the best in **bold** and the second best underlined. The values in gray indicate that the colors cannot be easily distinguished.

PD: perceptual difference, ND: name difference, ACIE76: average CIE76 color difference, MCIE76: minimal CIE76 color difference, CL: chroma-lightness, BHDI: balanced harmony-discrimination index.

	Flat color assignment						
Methods		Discriminability				Harmony	
	PD	ND.	ACIE76	MCIE76	Hue	CL	BHDI
Palettailor Color Crafting Tree Colors Cuttlefish	19.419 2.549 6.168 9.944	0.913 0.261 0.848 0.813	96.696 25.253 75.599 54.549	30.104 4.548 11.903 18.005	0.296 1.000 0.608 0.702	0.377 1.000 1.000 1.000	4.441 2.777 3.909 4.323
$Ours-D$ Ours-S	23.194 23.070	0.921 0.920	79.968 79.742	30.594 30.495	0.876 0.893	0.955 0.962	5.992 6.002

Table S5: Comparison of our method with the representative color assignment methods for hierarchical color assignment, with the best in bold and the second best underlined. The values in gray indicate that the colors cannot be easily distinguished.

PD: perceptual difference, ND: name difference, ACIE76: average CIE76 color difference, MCIE76: minimal CIE76 color difference, CL: chroma-lightness, BHDI: balanced harmony-discrimination index, SS: silhouette score, DR: distance ratio, RoMM: ratio of the maximum color distance between siblings to the minimum color distance between cousins.

		Hierarchical color assignment								
Methods		Discriminability				Harmony		Alignment with hierarchy		
	PD	ND.	ACIE76	MCIE76	Hue	CL	BHDI	SS	DR	RoMM
Palettailor Color Crafting Tree Colors Cuttlefish	8.202 4.176 0.226 4.615	0.508 0.243 0.066 0.382	51.697 23.015 6.959 25.248	16.102 8.143 0.379 8.497	0.838 0.997 0.978 0.606	0.579 0.998 000.1 1.000	3.253 2.898 2.133 2.832	0.582 0.642 0.785 0.715	0.883 0.930 0.994 0.907	6.471×10^{5} 3.038 4.370×10^{3} 0.972
Ours-D Ours-S	16.579 16.482	0.736 0.699	53.552 48.635	23.862 20.852	0.984 0.985	0.810 0.927	4.926 4.958	0.740 0.740	0.945 0.946	0.527 0.538

4 QUANTITATIVE EVALUATION WITH ADDITIONAL MEASURES

In this section, we present the comparison results using three additional measures: average CIE76 color difference (ACIE76), minimal CIE76 color difference (MCIE76), and the ratio of the maximum color distance between siblings to the minimum color distance between cousins (RoMM). ACIE76 and MCIE76 are commonly used measures for color discriminability [\[15\]](#page-5-20) and are not used in our optimization process. RoMM evaluates the alignment with hierarchy, where a lower RoMM indicates that the colors under the same parents have more similar colors.

Tables [S4](#page-2-0) and [S5](#page-2-1) provide a comparative analysis of the flat and hierarchical color assignment, respectively. In the flat color assignment, Ours-D performs the best in MCIE76 and ranks second to Paletailor [\[12\]](#page-5-15) in ACIE76. However, it should be noted that Paletailor achieves its high ACIE76 score by using a much broader chroma range $([0,100]$ *vs.* ours [40,85]). This broader range results in the inclusion of extreme colors, such as dim colors with low chroma (see colors \blacksquare in Fig [S4\(](#page-1-3)a)). Consequently, Paletailor records the lowest harmony scores, with 0.296 in Hue and 0.377 in CL, indicating a significant compromise in color harmony. In the hierarchical color assignment, Ours-D performs the best in all three additional measures. Cuttlefish [\[19\]](#page-5-16) also shows better performance in RoMM by maintaining hue consistency between colors of the same parent. However, it still performs worse than our methods, which employ constraints in dynamic range selection to ensure color compactness under the same parent and sufficient separation across different parents. In addition, Cuttlefish may still produce similar colors when there are too many subclasses due to the limited use of lightness and chroma $(e.g.,$ colors in Fig [S4\(](#page-1-3)d)). This limitation is also evidenced by its lower scores in discriminability (4.615 in PD and 8.497 in MCIE76).

5 ADDITIONAL RESULTS OF USER STUDY

In this section, we provide additional results from the user study, including the distribution of the ranks and frequency of the methods that are ranked first. Similar conclusions to those obtained in the paper can be drawn based on these graphical results.

Distribution of the ranks. As shown in [Fig. S5,](#page-2-2) it can be seen that, overall, our method performs the best, followed by Cuttlefish [\[19\]](#page-5-16). This indicates the advantage of dynamic methods in handling data under hierarchy. [Fig. S6](#page-3-0) shows the performance on the discriminability task, where our method outperforms all other methods, with Palettailor [\[12\]](#page-5-15) coming next as it focuses on optimizing distinctiveness. [Fig. S7](#page-3-1) demonstrates the performance on the harmony task, where our method approaches Cuttlefish and outperforms other methods. [Fig. S8](#page-3-2) illustrates the performance on the alignment with the hierarchy task, where our method outperforms all other methods.

Ratios of methods that are ranked highest. In addition, we analyze which methods users most often rank as their first choice across various trials. The results are summarized in [Figs. S9](#page-4-0) to [S12.](#page-4-0) It is observed that users generally prefer our method and rank it as their first choice. Regarding harmony, Cuttlefish, and our method are comparable, which is consistent with the findings we draw earlier. Specifically, as illustrated in [Fig. S12,](#page-4-0) our method demonstrates excellent alignment with the hierarchy even at the lower level.

Fig. S5: The distribution of the ranks of different methods on all the three tasks

Fig. S6: The distribution of the ranks of different methods on the task of discriminability.

Fig. S7: The distribution of the ranks of different methods on the task of harmony.

Fig. S8: The distribution of the ranks of different methods on the task of alignment with hierarchy.

Fig. S9: The frequency of the methods that are ranked first under all the three exploration scenarios.

Fig. S10: The frequency of the methods that are ranked first under the exploration scenario that users examine a higher hierarchical level with a balanced subclass distribution.

Fig. S11: The frequency of the methods that are ranked first under the exploration scenario that users examine a higher hierarchical level with an imbalanced subclass distribution.

Fig. S12: The frequency of the methods that are ranked first under the exploration scenario that users examine a lower hierarchical level, where the available color range will become much narrower.

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